

Faculty of information technology  
Department of System Analysis and Management



**Thesis**

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# **Analysis and optimization of resource costs in multi-stage rolling production**

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# The purpose of the research

**The object** of this research is a two-stage process of metal distribution when producing rolling products.

**The subject** is a mathematical model of steel consumption minimization considering the two-stage billets cutting and its program realization.

**The purpose** is achievement a decrease in resource costs in the multi-stage production of rolled products within a given plan through the development of the appropriate math apparatus and software.



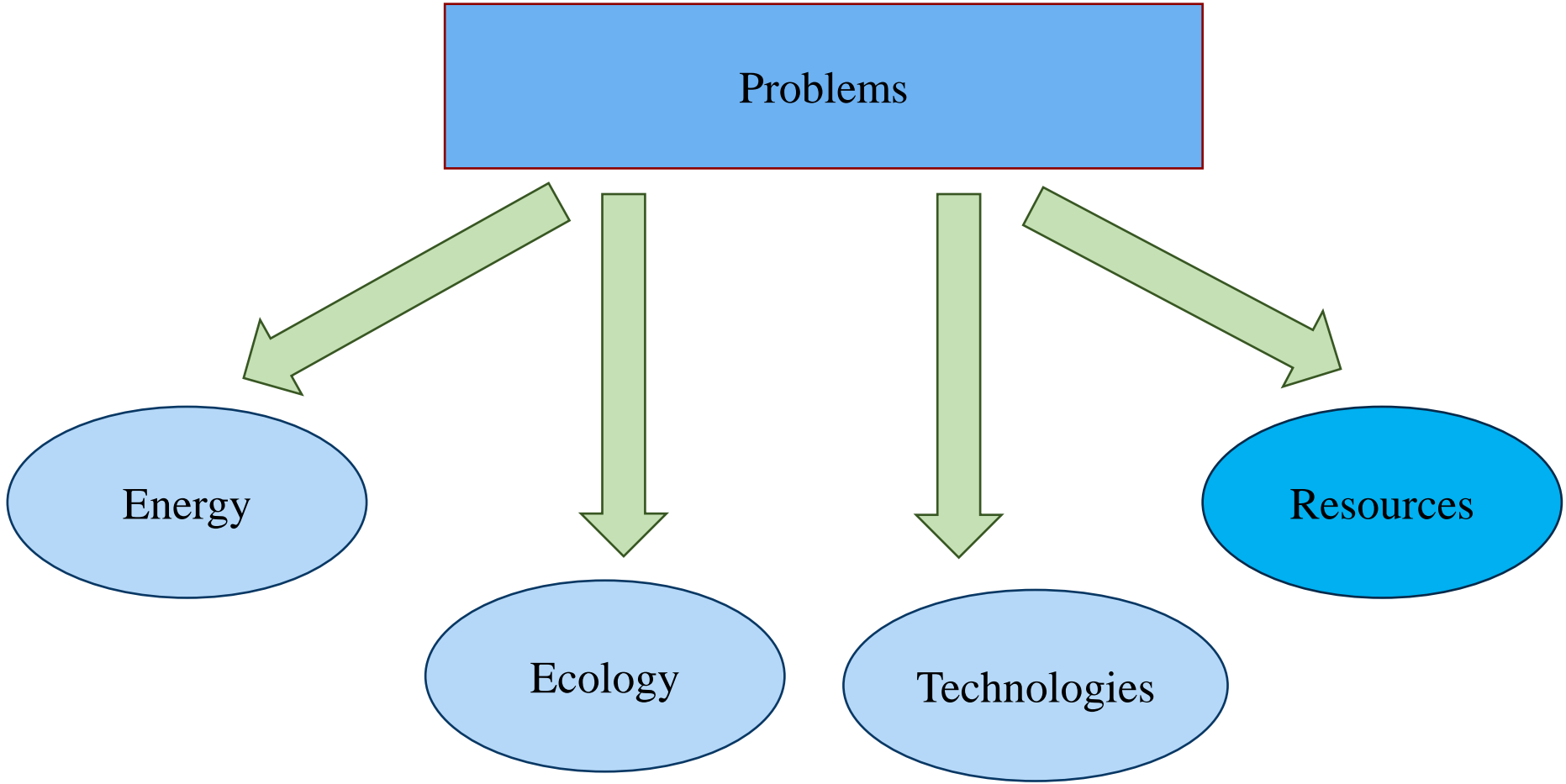
# The main problems

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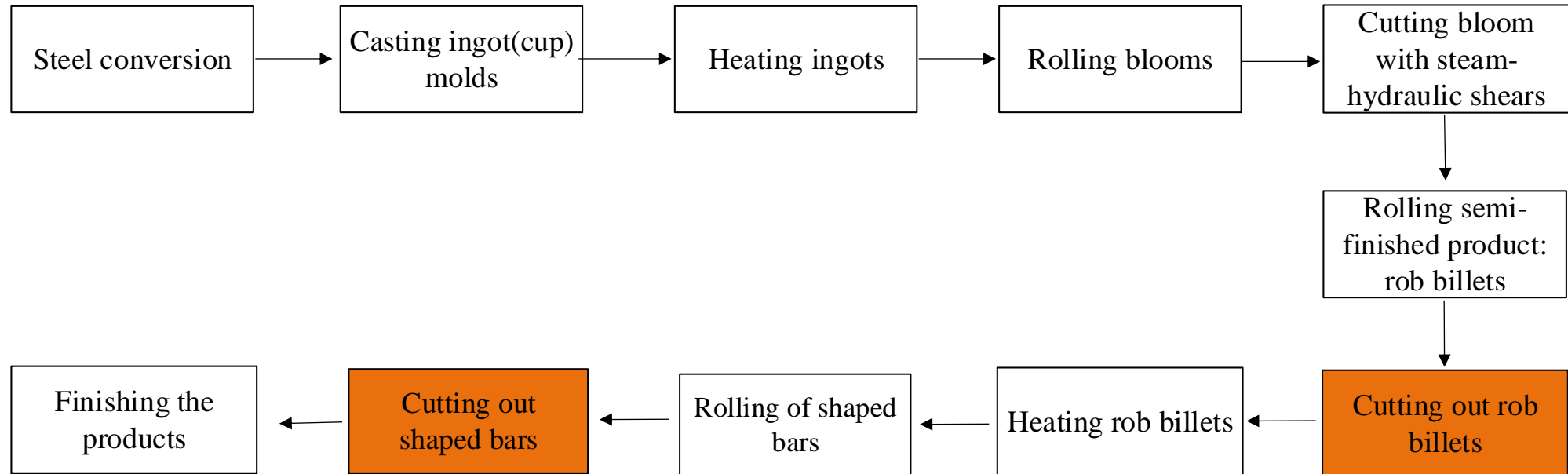
1. Analysis of different problems of rolled products
2. General scheme of the multi-stage production of rolled products
3. Math problem of steel consumption minimization considering the two-stage billets cutting
4. Processing of orders
5. Program realization of the math model
6. Analysis of results



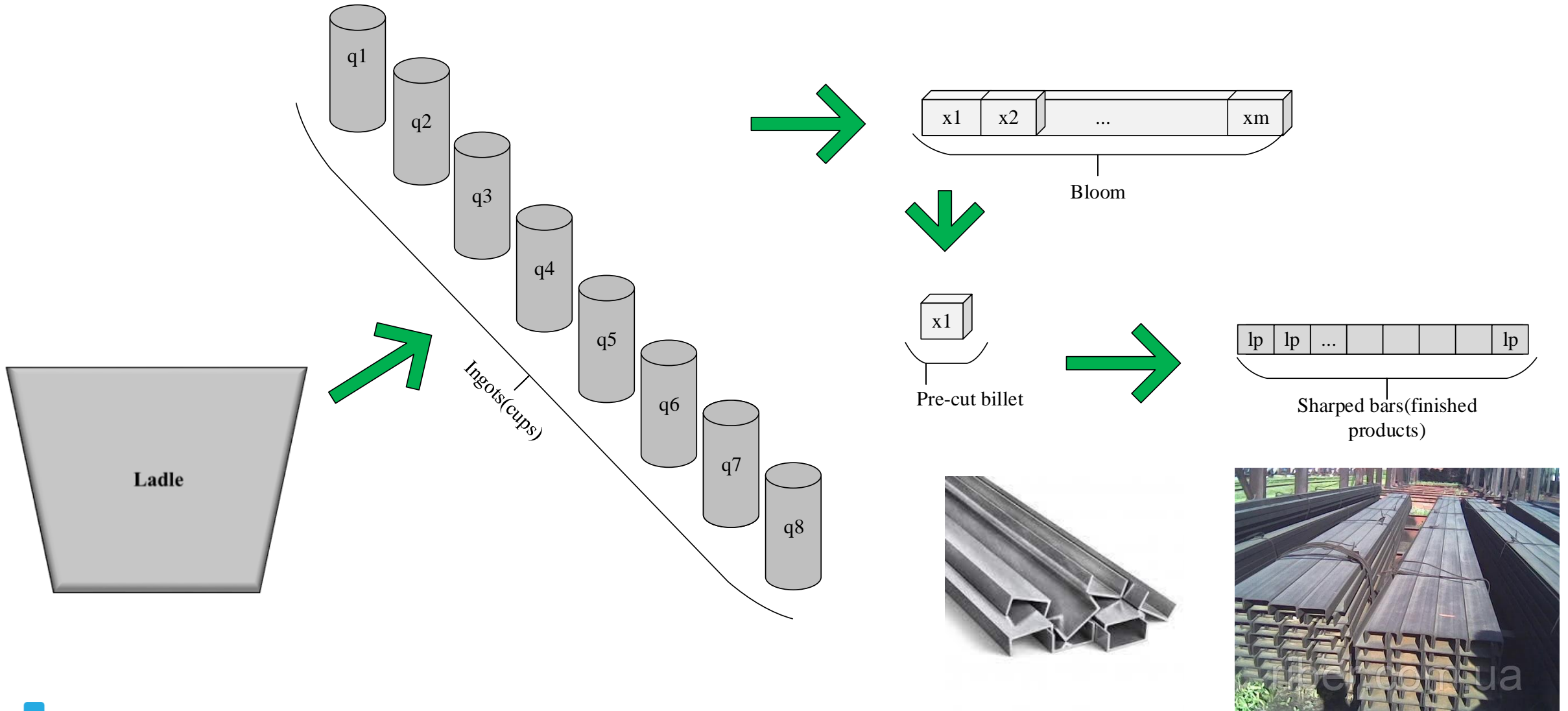
# Different problems in the production of rolled products



# Stage of technological process of graded rolled products



# The scheme with the entered designations in mathematical model



# Second-stage billets cutting

| Length of the final product, m | Mass of 1 running meter, kg | Optimal billet length, m | Cogged ingot length, m | Number of rods, pcs. | Cut-offs, m / % |      |
|--------------------------------|-----------------------------|--------------------------|------------------------|----------------------|-----------------|------|
| 11,7                           | 7,034                       | 2,85                     | 47,2                   | 4                    | 0,44            | 0,94 |
| 12,0                           | 7,034                       | 2,90                     | 48,1                   | 4                    | 0,07            | 0,15 |
| 9,0                            | 7,034                       | 2,75                     | 45,6                   | 5                    | 0,58            | 1,28 |
| 6,0                            | 7,034                       | 2,90                     | 48,1                   | 8                    | 0,07            | 0,15 |

Optimal length of a pre-cut billet of channel 8U depending on the rod length





# First-stage billets cutting

$$\begin{aligned} \text{minimize } Z(q, x) = \sum_{n=1}^N \left( l_n - \sum_{m=\overline{1, M}: \sigma_{nm}=1} \sum_{p=1}^4 \text{length}_m^p \cdot x_m^{p,n} \right) \\ q_1 + q_2 + \dots + q_n \leq Q; \end{aligned} \quad (1)$$

$$\sum_{n=1}^N x_m^{p,n} = \text{Number\_Zag}_m^p, \quad m = \overline{1, 2, \dots, M}; p = 1, 2, 3, 4; \quad (2)$$

$$\sum_{m=\overline{1, M}: \sigma_{nm}=1} \sum_{p=1}^4 \text{length}_m^p \cdot x_m^{p,n} - \frac{q_n}{a_n c_n \rho} \leq 0, n = 1, 2, \dots, N; \quad (3)$$

$$q_{\min} \leq q_n \leq q_{\max}, n = 1, 2, \dots, N; \quad (4)$$

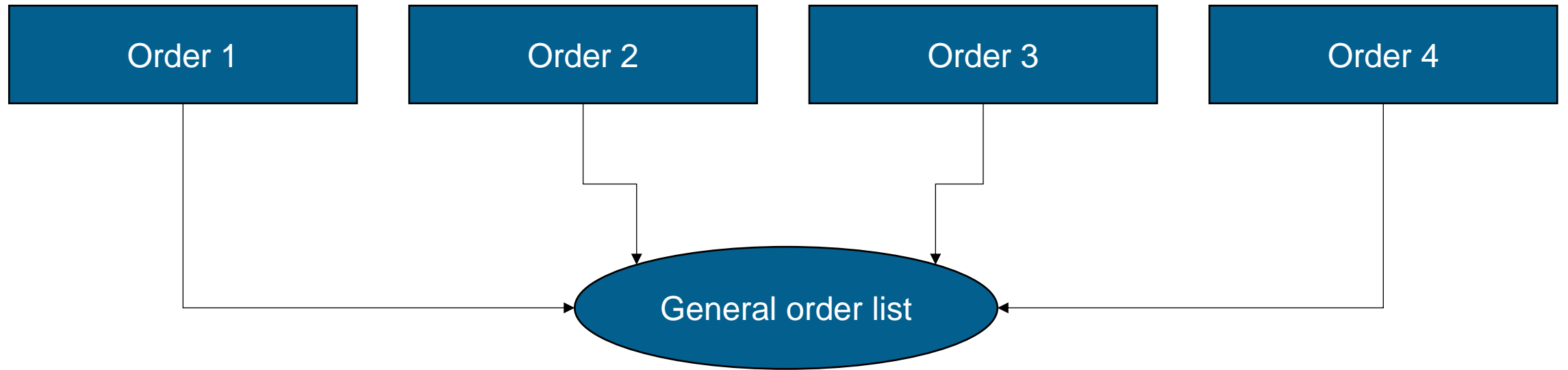
$$x_m^{p,n} \geq 0, x_m^{p,n} - \text{цїлі}, p = 1, 2, 3, 4; m = \overline{1, M}; n = \overline{1, N}; \sigma_{nm} = 1. \quad (5)$$

$$\text{Number\_Zag}_m^p = \frac{b_m^p}{\text{amount}_m^p}, m = 1, 2, \dots, M; p = 1, 2, 3, 4 \quad (6)$$





# Order



| Channel № | Length(m) | Mass (t) |
|-----------|-----------|----------|
| 8         | 12        | 10       |
| 12        | 12        | 23       |
| 14        | 11,7      | 10       |
| 10        | 6         | 10       |



# Order processing

| Channel № | Length(m) | Mass (t) |
|-----------|-----------|----------|
| 8         | 9         | 44       |
| 8         | 12        | 10       |
| 10        | 11.7      | 20       |
| 10        | 12        | 25       |
| 10        | 6         | 10       |
| 10        | 9         | 15       |
| 12        | 6         | 105      |
| 12        | 9         | 20       |
| 12        | 12        | 23       |
| 14        | 11.7      | 37       |

| Channel № | Length(m) | Mass (t) |
|-----------|-----------|----------|
| 12        | 6         | 52.5     |

| Channel № | Length(m) | Mass (t) |
|-----------|-----------|----------|
| 8         | 9         | 44       |
| 8         | 12        | 10       |

| Channel № | Length(m) | Mass (t) |
|-----------|-----------|----------|
| 10        | 11.7      | 20       |
| 10        | 6         | 10       |
| 10        | 9         | 15       |



# First-stage billets cutting

| Channel № | Length(m) | Mass (t) | Plan(pcs.) | Number of billets(pcs.) |
|-----------|-----------|----------|------------|-------------------------|
| 8         | 9         | 44       | 695        | 139                     |
| 8         | 12        | 10       | 116        | 29                      |

$$F = \frac{1}{0.125 \cdot 0.125 \cdot 7856} q_1 + \dots + \frac{1}{0.125 \cdot 0.125 \cdot 7856} q_8 - 2,75 * x_1^1 - 2,9 * x_1^2 - 2,75 * x_2^1 - 2,9 * x_2^2 - \dots - 2,75 * x_8^1 - 2,9 * x_8^2 \rightarrow \min$$

$$\left\{ \begin{array}{l} q_1 + \dots + q_8 \leq 60000 \\ x_1^1 + \dots + x_8^1 = 139 \\ x_1^2 + \dots + x_8^2 = 29 \\ \frac{1}{0.125 * 0.125 * 7856} q_1 - 2.75 * x_1^1 - 2.9 * x_1^2 \geq 0 \\ \dots \\ \frac{1}{0.125 * 0.125 * 7856} q_8 - 2.75 * x_8^1 - 2.9 * x_8^2 \geq 0 \\ 4400 \leq q_1, \dots, q_8 \leq 7400 \\ x_1^1, \dots, x_8^1, x_1^2, \dots, x_8^2 - \text{цілі} \end{array} \right.$$

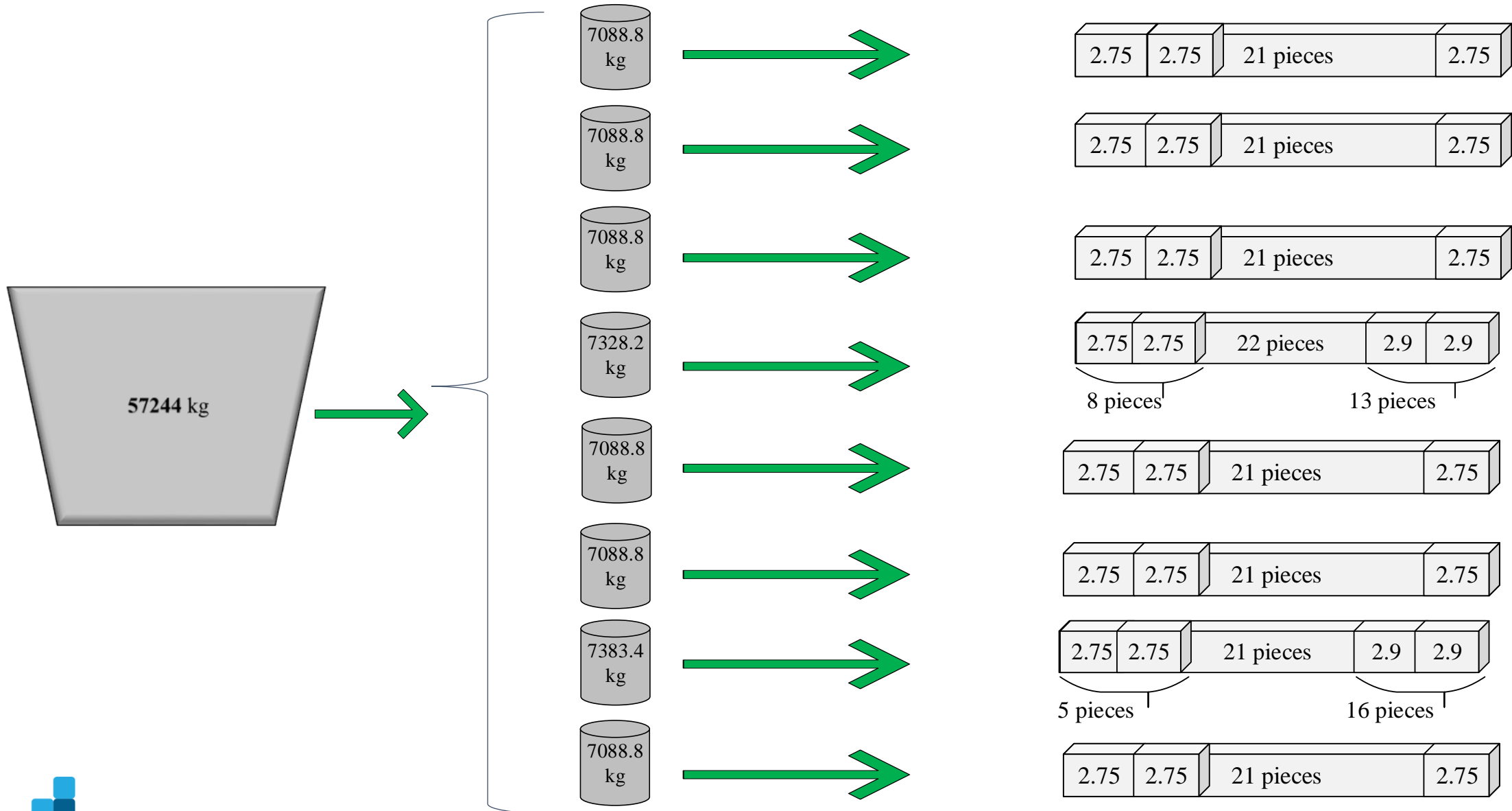
# Analysis of results

| n | $a_n(m)$ | $c_n(m)$ | $q_n(kg)$ | $x_{1n}(pcs.)$ | $x_{2n}(pcs.)$ |
|---|----------|----------|-----------|----------------|----------------|
| 1 | 0.125    | 0.125    | 7088.8    | 21             | 0              |
| 2 | 0.125    | 0.125    | 7088.8    | 21             | 0              |
| 3 | 0.125    | 0.125    | 7088.8    | 21             | 0              |
| 4 | 0.125    | 0.125    | 7328.2    | 8              | 13             |
| 5 | 0.125    | 0.125    | 7088.8    | 21             | 0              |
| 6 | 0.125    | 0.125    | 7088.8    | 21             | 0              |
| 7 | 0.125    | 0.125    | 7383.4    | 5              | 16             |
| 8 | 0.125    | 0.125    | 7088.8    | 21             | 0              |

The amount of metal in the blooms is 57244 kg, and therefore the excess production is 5.67%, which means that the order, firstly, is fulfilled, and secondly, the answer is optimal.



# The result of optimization of the first stage of cutting(subtask 2)



# Conclusion

| Number of parts | Total mass of part of order (kg) | The resulting mass of metal fed into the ladle (kg) | Difference (%) |
|-----------------|----------------------------------|---|----------------|
| 1               | 54000                            | 57244   | 5,67           |
| 2               | 45000                            | 46840   | 3,93           |
| 3, 4            | 52500                            | 55794   | 5,9            |
| 5               | 47000                            | 49610   | 5,26           |
| 6               | 51000                            | 53196   | 4,13           |
| 7               | 47000                            | 49440   | 4,94           |

$$Mean\% = \frac{57244 \cdot 5,67 + 46840 \cdot 3,93 + \dots + 49440 \cdot 4,94}{57244 + 46840 + \dots + 49440} = 5,01\%$$

Since in practice the value is allowed up to 10%, it can be concluded that the developed mathematical model and its software implementation allows to solve the problem of overconsumption of metal during the production of metallurgical plants and quantitatively justify the relevant decisions. Modification of the model is possible, due to the specification of the objective function and constraints.

